# Why are transmission gratings less angle sensitive than reflection gratings? 

## Technical Note



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## Introduction

Anyone who has tried to align both transmission gratings and reflection gratings will have experienced that the transmission grating is much easier to align. But, what is the physics behind that? One would think that the diffracted orders of both types of gratings are determined by the same grating equation so, why is there still a difference? This technical note will explain the reason for the difference in angular alignment tolerance between transmission and reflection gratings.

## High level explanation

The main difference can be seen on the figures above. In the following, all angles are measured relative to the normal of the grating. First we will consider the $0^{\text {th }}$ order diffraction order for both types of gratings while tilting the grating slightly. For the $0^{\text {th }}$ order diffraction the diffraction angle ( $\beta$ ) equals the angle of incidence $(\alpha)$. For a reflective grating, the $0^{\text {th }}$ order is obviously reflected back from the surface just as if the grating was a plane mirror so, when the grating is tilted the $0^{\text {th }}$ order diffraction shifts by twice the angular tilt. The higher order diffractions basically follow the $0^{\text {th }}$ order diffraction so, the $\mathrm{m}^{\text {th }}$ order diffraction also shifts angularly by twice the tilt angle of the grating. For a transmission grating however, the $0^{\text {th }}$ order goes straight through the grating and is not affected by tilting the grating. Again, since the higher order diffractions follow the $0^{\text {th }}$ order diffraction, the $\mathrm{m}^{\text {th }}$ order diffraction is almost unaffected by tilting the grating. Figure 1 compares the total change in $1^{\text {st }}$ order deflection angle for a transmission and reflection grating compared to the change of the $0^{\text {th }}$ order for a typical grating groove density of $1200 \mathrm{l} / \mathrm{mm}$. The plots in Figure 1 were calculated by the grating equation (see next Section for details).


Figure 1: Change of deflection angle for $0^{\text {th }}$ and $1^{\text {st }}$ order as a function of grating tilt for a transmission grating and reflection with grating 1200 I/mm.

## The equations

In order to calculate the actual deflection angles one has to consider the grating equation and add a tilt to the grating normal. The general grating equation that determines the relation between angle of incidence ( $\alpha$ ), diffraction angle ( $\beta$ ), the wavelength of light ( $\lambda$ ), and the period ( $\Lambda$ ) reads:

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m \lambda / \Lambda=\sin (\alpha)+\sin (\beta) \quad \text { Eq. } 1
$$

where $m$ is the diffraction order ( $0,-1,+1,-2,+2$, etc.). We will use Figure 2 in order to find the relation between the diffraction angle $\beta^{\prime \prime}$ as a function of tilt angle $\theta$. $\beta^{\prime \prime}$ is measured from the non-tilted grating normal. Angles on the left side of the grating are positive when measured counterclockwise. For the transmission grating the angles of transmitted orders are positive below the grating normal.

When the grating is tilted in the incoming beam by an angle $\theta$, the angle of incidence is reduced to $\alpha^{\prime}=\alpha-\theta$. The new diffraction angle ( $\beta^{\prime}$ ) is now measured from the tilted grating normal. From Figure 2 it can be seen that angle $\beta^{\prime \prime}$ - which is the new diffraction angle measured from the non-tilted grating normal becomes $\beta^{\prime \prime}=\beta^{\prime}-\theta$ for a transmission grating but $\beta^{\prime \prime}=\beta^{\prime}+\theta$ for a reflection grating. By inserting the grating equation and $\alpha^{\prime}=\alpha-\theta$ we get the following equation for calculation of $\beta^{\prime \prime}$ as a function of grating tilt:

Transmission grating: $\quad \beta^{\prime \prime}=\operatorname{asin}(m \lambda / \Lambda-\sin (\alpha-\theta))-\theta$
Reflection grating: $\quad \beta^{\prime \prime}=\operatorname{asin}(m \lambda / \Lambda-\sin (\alpha-\theta))+\theta$
These equations were used to calculate the deflection change $\beta^{\prime \prime}-\beta$ in Figure 2.


Figure 2: Change of diffraction angles for a) a transmission grating and b) a reflection grating when the grating is tilted by an angle $\theta$.

